

**GURU NANAK INSTITUTE OF TECHNOLOGY**  
**An Autonomous Institute under MAKAUT**  
**2022**  
**FORMAL LANGUAGE AND AUTOMATA THEORY**  
**IT403**

TIME ALLOTTED: 3 Hrs

FULL MARKS: 70

*The figures in the margin indicate full marks.**Candidates are required to give their answers in their own words as far as practicable***GROUP – A****(Multiple Choice Type Questions)**Answer any **ten** from the following, choosing the correct alternative of each question: **10×1=10**

		Marks	CO No
1.	(i) For a give Moore Machine, Given Input='101010', thus the output would be of length: a)  Input +1 b)  Input  c)  Input -1 d) Cannot be predicted	1	CO4
	(ii) The compatibility graph is used in searching for a) Minimal closed covering b) All incompatible pairs c) Minimum number of edges d) Both (a) and (c)	1	CO2
	(iii) The regular expression representing the set of all strings {x, y} ending with XX & beginning with Y a) XX(X+Y)*Y b) Y(X+Y)*XX c) YY(X+Y)*X d) Y(XY)*XX	1	CO3
	(iv) Which of the following strings can be obtained by the language $L = \{a^i b^{2i} \mid i \geq 1\}$ a) aabbbb b) aabbba c) aaabbb d) bbaaaa	1	CO3
	(v) The solution of the equation $R=Q+RP$ is a) $R=QP^*$ b) $P=RQ^*$ c) $R=Q^*P$ d) None of the above	1	CO2
	(vi) In Moore machine if the input string is of length n then output string is of length – a) n b) n/2 c) n+1 d) 2n	1	CO2

- (vii) According to the given table, compute the number of transitions with 1 as its symbol but not 0:

1 CO2

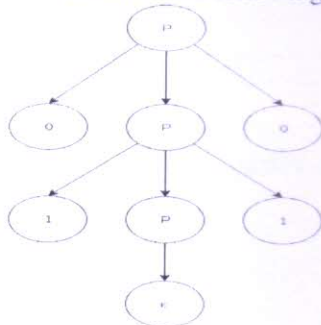
Q	$\Delta(q,0)$	$\delta(q,1)$
q0	{q0}	{q0, q1}
q1	{q2}	{q2}
q2	{q3}	{q3}
q3	$\Phi$	$\Phi$

- a) 4  
b) 3  
c) 2  
d) 1
- (viii) A grammar  $G=(V, T, P, S)$  is \_\_\_\_\_ if every production taken one of the two forms:  
 $B \rightarrow aC$   
 $B \rightarrow a$   
 a) Ambiguous  
 b) Regular  
 c) Non Regular  
 d) None of the mentioned

1 CO3

- (ix) Which of the following does the given parse tree correspond to?

1 CO5



- a)  $P \rightarrow 1100$   
 b)  $P \rightarrow 0110$   
 c)  $P \rightarrow 1100\varepsilon$   
 d)  $P \rightarrow 0101$
- (x) A context free grammar is a \_\_\_\_\_
- a) English grammar  
 b) Regular grammar  
 c) Context sensitive grammar  
 d) None of the mentioned

1 CO4

- (xi) Which among the following looks similar to the given expression?  $((0+1). (0+1))^*$
- a)  $\{x \in \{0,1\}^* | x \text{ is all binary number with even length}\}$   
 b)  $\{x \in \{0,1\}^* | x \text{ is all binary number with even length}\}$   
 c)  $\{x \in \{0,1\}^* | x \text{ is all binary number with odd length}\}$   
 d)  $\{x \in \{0,1\}^* | x \text{ is all binary number with odd length}\}$

1 CO2

- (xii) In Moore machine, output is produced over the change of:
- Transitions
  - States
  - all of the mentioned
  - none of the mentioned

1 CO1

## GROUP – B

(Short Answer Type Questions)

Answer any *three* from the following:  $3 \times 5 = 15$ 

Marks CO No

2. (a) Convert the following Moore machine into Mealy machine:

3 CO1

PRESENT STATE	NEXT STATE		OUTPUT
	a=0	a=1	
$\rightarrow q_1$	$q_1$	$q_2$	0
$q_2$	$q_1$	$q_3$	0
$q_3$	$q_1$	$q_3$	1

- (b) Simplify the given grammar:

2 CO1

 $S \rightarrow aXb$  $X \rightarrow aXb \mid \epsilon$ 

3. (a) Consider the following grammar:

3 CO2

 $S \rightarrow 0B/1A, A \rightarrow 0/0S/1AA, B \rightarrow 1/1S/0BB.$ 

For the string 00110101,

Find the leftmost derivation

- (b) Draw the derivation tree for the above derivation.

2 CO2

4. (a) Consider the following CFG:

4 CO1

 $S \rightarrow aaB, A \rightarrow bBb/\epsilon, B \rightarrow Aa.$ 

Find the parse tree for the string "aabbababa"

- (b) What is Ambiguous grammar?

1 CO3

5. Construct a minimum state automaton equivalent to a DFA whose transition table is given below (where  $q_3$  and  $q_4$  are two final states):

5 CO1

Present State	Next State	
	a=0	a=1
$\rightarrow q_0$	$q_1$	$q_2$
$q_1$	$q_4$	$q_3$
$q_2$	$q_4$	$q_3$
$q_3$	$q_5$	$q_6$
$q_4$	$q_7$	$q_6$
$q_5$	$q_3$	$q_6$
$q_6$	$q_6$	$q_6$
$q_7$	$q_4$	$q_6$

6. State and Prove the Arden's Theorem.

5 CO3

## GROUP - C

(Long Answer Type Questions)

Answer any *three* from the following:  $3 \times 15 = 45$ 

- |    |     |  | Marks | CO No |
|----|-----|--|-------|-------|
| 7. | (a) | Prove that $(1+00^*1) + (1+00^*1)(0+10^*1)^*(0+10^*1) = 0^*1(0+10^*1)^*$ .                                     | 4     | CO3   |
|    | (b) | Define Left factoring & Left recursion with proper example.  | 5     | CO1   |
|    | (c) | Convert the following grammar to GNF<br>$S \rightarrow AB, \quad A \rightarrow BS/a, \quad B \rightarrow SA/b$ | 6     | CO4   |
| 8. | (a) | Find the equivalence class partition of the machine shown below:   | 9     | CO2   |

PRESENT STATE	NEXT STATE, z	
	x=0	x=1
A	E,0	D,1
B	F,0	D,0
C	E,0	B,1
D	F,0	B,0
E	C,0	F,1
F	B,0	C,0

- |    |     |   |   |     |
|----|-----|---|---|-----|
|    | (b) | Show a standard form of the corresponding reduced machine for the above machine | 6 | CO4 |
| 9. | (a) | Convert the following Mealy machine into Moore machine:                         | 5 | CO2 |

PRESENT STATE	NEXT STATE			
	a=0		a=1	
	STATE	OUTPUT	STATE	OUTPUT
$\rightarrow q_1$	$q_3$	0	$q_2$	0
$q_2$	$q_1$	1	$q_4$	0
$q_3$	$q_2$	1	$q_1$	1
$q_4$	$q_4$	1	$q_3$	0

- |  |     |  |   |     |
|--|-----|--|---|-----|
|  | (b) | Consider the following table and find a minimum length sequence that distinguishes state A from state B. | 4 | CO2 |
|--|-----|--|---|-----|

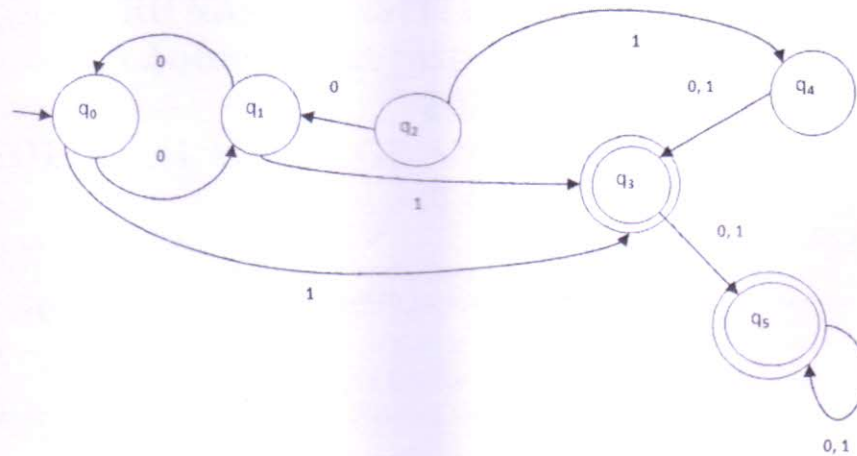
PRESENT STATE	NEXT STATE, z	
	x=0	x=1
A	B,1	H,1
B	F,1	D,1
C	D,0	E,1
D	C,0	F,1
E	D,1	C,1
F	C,1	C,1
G	C,1	D,1
H	C,0	A,1



(c) Minimize the states in the DFA depicted in the following diagram:

6

CO1



- |     |     |   |        |     |
|-----|-----|---|--------|-----|
| 10. | (a) | Find the CFG for the given Language:<br>$L = \{x \in \{0,1\}^* \mid \text{number of zeroes in } x = \text{number of one's in } x\}$ | 5      | CO5 |
|     | (b) | Construct a push down automata for the language $L = \{ww^R \mid w \in \{a,b\}^*\}$   | 6      | CO3 |
|     | (c) | Using Pumping Lemma check whether $L = \{a^n b^n \mid n \geq 1\}$ is regular or not.  | 4      | CO3 |
| 11. |     | Write short notes on any three of the followings:   | 3x5=15 |     |
|     | (a) | Ambiguity and Inherent Ambiguity  | 5      | CO4 |
|     | (b) | Turing machine  | 5      | CO1 |
|     | (c) | Pumping lemma for Regular Set   | 5      | CO2 |
|     | (d) | Classification of languages and their relations   | 5      | CO2 |
|     | (e) | Merger Graph  | 5      | CO3 |