

**GURU NANAK INSTITUTE OF TECHNOLOGY**  
**An Autonomous Institute under MAKAUT**  
**2021**  
**SIGNALS AND SYSTEMS (Backlog)**  
**EC401**

TIME ALLOTTED: 3 HOURS

FULL MARKS: 70

*The figures in the margin indicate full marks.*

*Candidates are required to give their answers in their own words as far as practicable*

**GROUP – A**

**(Multiple Choice Type Questions)**

Answer any **ten** from the following, choosing the correct alternative of each question: **10×1=10**

		Marks	CO No
1.	(i) The signal $x(n)=(1/2)^n u(n)$ is a) Power signal b) Energy Signal c) Both Energy and Power signal d) None of these	1	CO2
	(ii) The system $y[n] = \sin(x[n])$ is a) Periodic b) Aperiodic c) Causal d) Noncausal	1	CO2
	(iii) The Fourier coefficient $a_n$ can be evaluated as a) $\frac{2}{T} \int_0^T x(t) \cos n\omega t dt$ b) $\frac{2}{T} \int_{-\alpha}^{\alpha} x(t) \cos n\omega t dt$ c) $\frac{2}{T} \int_{-T/2}^{T/2} x(t) \cos n\omega t dt$ d) $\frac{2}{T} \int_0^{\alpha} x(t) \cos n\omega t dt$	1	CO2
	(iv) Check the system $y[n] = x[n] - x[n-2]$ is a) With memory b) Without memory c) With small memory d) None	1	CO2
	(v) If $x(t)$ is odd, then its Fourier series coefficients must be a) Real and odd b) imaginary and odd c) real and even d) imaginary and even	1	CO2
	(vi) A linear discrete-time system has the characteristic equation $z^3 - 0.81z = 0$ . The system a) is stable b) is marginally stable c) is unstable d) limitedly stable	01	CO4

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|--------|--|---|-----|
| (vii)  | The type of systems which are characterized by input and the output quantized at certain levels are called as<br>a) analog<br>b) discrete<br>c) continuous<br>d) digital   | 1 | CO5 |
| (viii) | The Fourier transform of a rectangular pulse is<br>a) Impulse<br>b) Triangular pulse<br>c) Sine function<br>d) Sinc function   | 1 | CO3 |
| (ix)   | The Z-Transform $X(z)$ of a discrete time signal $x(n)$ is defined as:<br>a) $\sum_{n=-\infty}^{\infty} x(n)z^n$<br>b) $\sum_{n=-\infty}^{\infty} x(n)z^{-n}$<br>c) $\sum_{n=0}^{\infty} x(n)z^n$<br>d) None of the mentioned  | 1 | CO4 |
| (x)    | What is the ROC of the signal $x(n)=\delta(n-k), k>0$ ?<br>a) $z=0$<br>b) $z=\infty$<br>c) Entire $z$ -plane, except at $z=0$<br>d) Entire $z$ -plane, except at $z=\infty$  | 1 | CO3 |
| (xi)   | The similarity between the Fourier transform and the $z$ transform is that<br>a) Both convert frequency spectrum domain to discrete time domain<br>b) Both convert discrete time domain to frequency spectrum domain<br>c) Both convert analog signal to digital signal<br>d) Both convert digital signal to analog signal | 1 | CO4 |
| (xii)  | A variable that can assume any value between two given points is called<br>a) Continuous random variable<br>b) Discrete random variable<br>c) Irregular random variable<br>d) Uncertain random variable  | 1 |     |

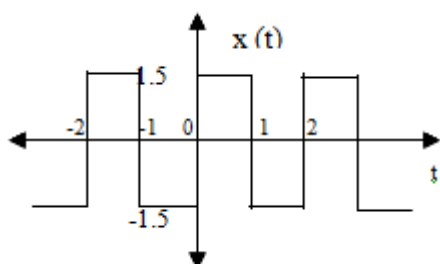
**GROUP – B****(Short Answer Type Questions)**Answer any **three** from the following: **3×5=15**

- |    |  | Marks | CO No |
|----|--|-------|-------|
| 2. | (a) State the condition for existence of Fourier series. | 2     | CO2   |
|    | (b) What is aliasing? What is an anti-aliasing filter?   | 3     | CO5   |
|    | Find even and odd component of the signal                | 3     | CO1   |
| 3. | (a) $x(n)=\{-2, \underset{\uparrow}{1}, 2, -1, 3\}$      |       |       |

- (b) A continuous time signal is defined as  $x(t) = e^{-at}$ ,  $a > 0$  Find the Fourier Transform of  $x(t)$ . 2 CO3
- If  $x(n)$  is causal sequence which is shifted by 'm' amount, prove that
4. (a)  $z\{x(n-m)\} = z^{-m}\{X_+(z) + \sum_{k=1}^m x(-k)z^k\}$ . 5 CO3
- Find the Nyquist rate of
5. (a) i)  $7\sin 800\pi t - 5\cos 600\pi t - 10\sin 1800\pi t$  5 CO1  
 ii)  $-2.5\sin(800\pi t) \times \cos(600\pi t)$
6. Sketch the following signal and calculate their energies
- i.  $e^{-10t} u(t)$  5 CO1  
 ii.  $u(t) - u(t-15)$  CO1

**GROUP – C****(Long Answer Type Questions)**Answer any *three* from the following: **3×15=45**

- |        |  | Marks | CO No    |
|--------|--|-------|----------|
| 7. (a) | Discuss the importance of convolution sum.   | 3     | CO2      |
| (b)    | Prove that if two systems are connected in parallel the overall impulse response is equal to sum of two impulse responses                      | 6     | CO2      |
| (c)    | Find the convolution of two sequences $x_1(n) = \{1, -1, 2, 3\}$<br>$x_2(n) = \{1, -2, 3, 1\}$ using Matrix method                             | 6     | CO2      |
| 8. (a) | State and prove initial and final value theorem of z-transform.  | 5     | CO4      |
| (b)    | Find the z-transform and ROC of the sequence<br>$x(n) = (1/2)^n u(-n)$   | 5     | CO4      |
| (c)    | Find the inverse Z transform of<br>$X(z) = \frac{z(z-1)}{(z+2)^3(z+1)}$<br>ROC: $ z  > 2$  | 5     | CO3      |
| 9. (a) | Check the followings for the system $y(n) = x(n+1) + 1/x(n+1)$<br>(i) Static & Dynamic<br>(ii) Linear & Nonlinear<br>(iii) Causal & Non-Causal | 6     | CO1, CO2 |
| (b)    | Explain the even symmetry and odd symmetry of Fourier series.  | 4     | CO3      |
| (c)    | Find the Fourier series coefficients for the continuous time periodic signal<br>$x(t) = 1.5$ for $0 \leq t < 1$<br>$= -1.5$ for $1 \leq t < 2$ |       |          |



5 CO3

- |     |     |   |        |     |
|-----|-----|---|--------|-----|
| 10. | (a) | Determine the convolution output of the two signals using graphical method. $x(n)=\{3,3,1,1\}$ and $h(n)=\{1,2,1,1\}$   | 7      | CO3 |
|     | (b) | Check whether the signal is causal or noncausal.<br>i) $y(t) = x(t)\cos(t+1)$ ii) $y(n) = x(n^3)$   | 4      | CO3 |
|     | (c) | Prove that the z-transform of convolution of $x(n)$ and $h(n)$ is the multiplication of z-transform of individual.<br>Write short notes on any three of the following | 4      | CO2 |
|     |     |   | 5x3=15 |     |
|     |     |   |        |     |
| 11. | (a) | Nyquist Sampling Theorem  | 5      | CO1 |
|     | (b) | Random variables  | 5      | CO5 |
|     | (c) | Difference between FT and DTFT  | 5      | CO3 |
|     | (d) | Invertible and Non-invertible System,   | 5      | CO4 |
|     | (e) | BIBO Stability  | 5      | CO3 |