

GURU NANAK INSTITUTE OF TECHNOLOGY
An Autonomous Institute under MAKAUT
2022
SIGNALS AND SYSTEMS
EC304

TIME ALLOTTED: 3Hours

FULL MARKS:70

*The figures in the margin indicate full marks.**Candidates are required to give their answers in their own words as far as practicable***GROUP – A****(Multiple Choice Type Questions)**Answer any **ten** from the following, choosing the correct alternative of each question: $10 \times 1 = 10$

		Marks	CO No
1.	i) Determine the Z transform of the function $x(n) = n25^n u(n)$	1	CO3
	a. $X(z) = 5z(z+5)/(z-5)^3$		
	b. $X(z) = 3z(z+5)/(z-5)^3$		
	c. $X(z) = 2z(z+3)/(z-5)^2$		
	d. $X(z) = 5z(z+5)/(z-5)^2$		
	ii) A time invariant system is a system whose output	1	CO1
	a. increases with a delay in input		
	b. decreases with a delay in input		
	c. remains same with a delay in input		
	d. vanishes with a delay in input		
	iii) Which of the following is not Dirichlet's condition for the Fourier series expansion?	1	CO3
	a. $f(x)$ is periodic, single valued, finite		
	b. $f(x)$ has finite number of discontinuities in only one period		
	c. $f(x)$ has finite number of maxima and minima		
	d. $f(x)$ is a periodic, single valued, finite		
	iv) For a system function $H(s)$ to be stable	1	CO1
	a. The zeros lie in left half of the s plane		
	b. The zeros lie in right half of the s plane		
	c. The poles lie in left half of the s plane		
	d. The poles lie in right half of the s plane		
	v) If a signal $f(t)$ has energy E, the energy of the signal $f(100t)$ is equal to _____	1	CO2
	a. E		
	b. 100E		
	c. E/100		
	d. 400E		
	vi) One of the types of signal is an Impulse train. The type of discontinuity in an impulse train is _____	1	CO2
	a. Infinite		
	b. Zero		
	c. One		
	d. Finite		

- vii) A periodic signal $x(t)$ of period T_0 is given by

$$x(t) = 1 \quad |t| < T_1$$

$$= 0 \quad T_1 < |t| < \frac{T_0}{2}$$
The dc component of $x(t)$ is
a. $\frac{T_1}{T_0}$
b. $\frac{T_1}{2T_0}$
c. $\frac{2T_1}{T_0}$
d. $\frac{T_0}{T_1}$ 1 CO2
- viii) The ROC of a system is the
a. range of z for which the z transform converges
b. range of frequency for which the z transform exists
c. range of frequency for which the signal gets transmitted
d. range in which the signal is free of noise 1 CO3
- ix) The region of convergence of the z -transform of a unit step function is
a. $|z| > 1$
b. $|z| < 1$
c. (Real part of z) > 0
d. (Real part of z) < 0 1 CO4
- x) The z -transform of the following real exponential sequence

$$x(n) = a^n n \geq 0$$

$$= 0 \quad \text{for } n < 0$$
is given by
a. $1 - az^{-1}; |z| > a$
b. $\frac{1}{1-az^{-1}}; |z| > a$
c. $-\frac{1}{1-az}; |z| > a$
d. $1 + az^{-1}; |z| < a$ 1 CO4
- xi) The discrete time system $y(n) = x(n-3) - 4x(n-10)$ is a
a. Time varying system
b. Dynamic system
c. Memoryless system
d. None of these 1 CO1
- xii) Determine the Time period of: $x(t) = 3 \cos(20t+5) + \sin(8t-3)$.
a. 1/10 sec
b. 1/20 sec
c. 2/5 sec
d. 2/4 sec 1 CO1

GROUP - B

(Short Answer Type Questions)

Answer any *three* from the following: $3 \times 5 = 15$

- | | | Marks | CO No |
|----|---|-------|-------|
| 2. | Determine whether the system $y(n) = (1/2)^n u(n)$ stable or unstable? | 5 | CO4 |
| 3. | What is time reversal operation on a signal and draw the following signal:
$u(n+2) - u(n-3)$ | 5 | CO2 |

- | | | | | |
|----|-----|---|---|-----|
| 4. | (a) | What is probability density function (PDF)? | 2 | CO5 |
| | (b) | Find the cross correlation of two finite length sequences $x(n)=\{1,2,1,1\}$ and $y(n)=\{1,2,1,1\}$ | 3 | CO3 |
| 5. | | Explain the properties of Region Of Convergence (ROC) of $X(z)$. | 5 | CO4 |
| 6. | | Determine the Fourier transform of the followings $x(t) = e^{-at}u(t)$ | 5 | CO3 |

GROUP – C

(Long Answer Type Questions)

Answer any **three** from the following: $3 \times 15 = 45$

- | | | | Marks | CO No |
|-----|-----|--|--------|-------|
| 7. | (a) | Find the Nyquist rate of $9\cos(80\pi t) - 5\cos(60\pi t) - 10\sin(480\pi t)$ | 5 | CO1 |
| | (b) | Explain with example the time invariant and time invariant system. | 5 | CO1 |
| | (c) | Check whether the following systems are static or dynamic
i) $y(n)=x(n)x(n-1)$
ii) $y(n)=x^2(n)+x(n)$ | 5 | CO2 |
| 8. | (a) | Explain if the system described is causal or non-causal
$y(n) = x(n) + \frac{1}{x(n-1)}$ | 5 | CO2 |
| | (b) | Determine the convolution sum of two sequences:
$x(n) = \{1, 2, 0, 1\}$: $(n) = \{1, 1, 2, 0\}$
\uparrow | 5 | CO2 |
| | (c) | Find the discrete-time Fourier Transform of $x(n) = [3, -4, 5, 6]$ | 5 | CO3 |
| 9. | (a) | State and prove the sampling theorem with example | 4 | CO2 |
| | (b) | Find the Fourier series coefficients for the continuous time periodic signal.
$x(t) = 1.5 \quad \text{for } 0 \leq t \leq 1$
$= -1.5 \quad \text{for } 1 \leq t \leq 2$
with fundamental frequency $\Omega_0 = \pi$ | 6 | CO2 |
| | (c) | Determine the inverse z-transform of
$X(z) = \frac{1 + 2z^{-1}}{1 - 2z^{-1} + z^{-2}}$ | 5 | CO3 |
| 10. | (a) | State and prove initial and final value theorem of z-transform. | 5 | CO4 |
| | (b) | Determine the Z transform and ROC of the signal
$X(n) = a^n u(n) + b^n u(-n-1)$ | 7 | CO4 |
| | (c) | What do you mean by Exponential Fourier Series? | 3 | CO4 |
| 11. | | Write short notes on any three of the following: | 3x5=15 | |
| | (a) | Even and Odd signals | 5 | CO1 |
| | (b) | Initial value theorem | 5 | CO2 |
| | (c) | Gibb's phenomenon | 5 | CO3 |
| | (d) | Properties of continuous time Fourier transform | 5 | CO5 |
| | (e) | Periodic and aperiodic signal. | 5 | CO4 |